## Abstract

We establish a new energy inequality for the difference of two semi-convex functions in a bounded open convex set D of  $R^n$ .

This inequality is applied to the  $L^2$ - approximation problem of the gradient of the unknown solution of the nonlinear elliptic partial differential equation provided that the latter solution is a semi-convex function in D.